

## Single HEMG

$$fHEMGp1 := \left( \frac{1}{4 \cdot wI} \right) \cdot \exp \left( \left( \frac{x - w3}{wI} \right) + \frac{w\theta^2}{2 \cdot wI^2} \right) \cdot ERFC \cdot \left( \left( \frac{x - w3}{w\theta} \right) + \left( \frac{w\theta}{wI} \right) \right)$$

$$fHEMGp1 := \frac{e^{\frac{x - w3}{wI} + \frac{w\theta^2}{2 wI^2}} ERFC \left( \frac{x - w3}{w\theta} + \frac{w\theta}{wI} \right)}{4 wI} \quad (1.1)$$

$$dfHEMGp1 := diff(fHEMGp1, x)$$

$$dfHEMGp1 := \frac{e^{\frac{x - w3}{wI} + \frac{w\theta^2}{2 wI^2}} ERFC \left( \frac{x - w3}{w\theta} + \frac{w\theta}{wI} \right) + e^{\frac{x - w3}{wI} + \frac{w\theta^2}{2 wI^2}} ERFC \left( \frac{x - w3}{w\theta} + \frac{w\theta}{wI} \right)}{4 wI^2} \quad (1.2)$$

$$mfHEMGp1 := solve(dfHEMGp1 = 0, x)$$

$$mfHEMGp1 := -\frac{w\theta^2 + wI^2 - w3 wI}{wI} \quad (1.3)$$

## Additional HEMG

$$fHEMGp2 := \left( \frac{1}{4 \cdot w2} \right) \cdot \exp \left( \left( \frac{w3 - x}{w2} \right) + \frac{w\theta^2}{2 \cdot w2^2} \right) \cdot ERFC \cdot \left( \left( \frac{w3 - x}{w\theta} \right) + \left( \frac{w\theta}{w2} \right) \right)$$

$$fHEMGp2 := \frac{e^{\frac{w3 - x}{w2} + \frac{w\theta^2}{2 w2^2}} ERFC \left( \frac{w3 - x}{w\theta} + \frac{w\theta}{w2} \right)}{4 w2} \quad (2.1)$$

## Combined HEMG

$$\begin{aligned}
fHEMG &:= w4 \cdot (fHEMGP1 + fHEMGP2) + w5 \\
fHEMG &:= w4 \left( \frac{e^{\frac{x-w3}{wI} + \frac{w0^2}{2wI^2}} ERFC \left( \frac{x-w3}{w0} + \frac{w0}{wI} \right)}{4wI} \right. \\
&\quad \left. + \frac{e^{\frac{w3-x}{w2} + \frac{w0^2}{2w2^2}} ERFC \left( \frac{w3-x}{w0} + \frac{w0}{w2} \right)}{4w2} \right) + w5
\end{aligned} \tag{3.1}$$

$$\begin{aligned}
dfHEMGP &:= diff(fHEMG, x) \\
dfHEMGP &:= w4 \left( \frac{e^{\frac{x-w3}{wI} + \frac{w0^2}{2wI^2}} ERFC \left( \frac{x-w3}{w0} + \frac{w0}{wI} \right)}{4wI^2} + \frac{e^{\frac{x-w3}{wI} + \frac{w0^2}{2wI^2}} ERFC}{4wIw0} \right. \\
&\quad \left. - \frac{e^{\frac{w3-x}{w2} + \frac{w0^2}{2w2^2}} ERFC \left( \frac{w3-x}{w0} + \frac{w0}{w2} \right)}{4w2^2} - \frac{e^{\frac{w3-x}{w2} + \frac{w0^2}{2w2^2}} ERFC}{4w2w0} \right)
\end{aligned} \tag{3.2}$$

$$\begin{aligned}
mfHEMGP &:= solve(dfHEMGP = 0, x) \\
mfHEMGP &:= \frac{1}{2w2} \left( -2 \text{RootOf} \left( 2 e^{-Z} Z wI^3 w2^2 \right. \right. \\
&\quad \left. \left. - \frac{2 Z wI w2^2 - w0^2 wI - w0^2 w2}{2 w2 wI^2} \right. \right. \\
&\quad \left. \left. + 2 e^{-Z} wI w2^4 + e^{-Z} w0^2 wI^3 + 2 e^{-Z} wI^3 w2^2 \right. \right. \\
&\quad \left. \left. - \frac{2 Z wI w2^2 - w0^2 wI - w0^2 w2}{2 w2 wI^2} \right. \right. \\
&\quad \left. \left. - e^{-Z} w0^2 wI w2^2 - 2 e^{-Z} \frac{2 Z wI w2^2 - w0^2 wI - w0^2 w2}{2 w2 wI^2} w0^2 w2^3 \right. \right. \\
&\quad \left. \left. - 2 e^{-Z} \frac{2 Z wI w2^2 - w0^2 wI - w0^2 w2}{2 w2 wI^2} wI^2 w2^3 \right) w2^2 + w0^2 + 2 w3 w2 \right)
\end{aligned} \tag{3.3}$$